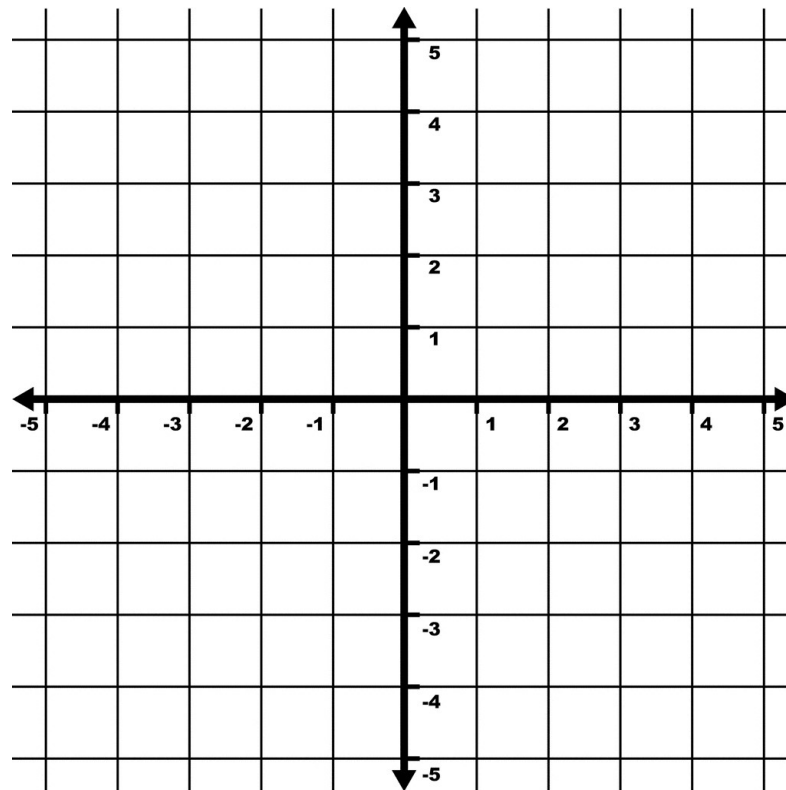


# Standard Form Review

$$2x + 3y = 6$$



5-6

## Parallel and Perpendicular Lines

### © Content Standard

**G.GPE.5** Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).

**I can determine whether lines are parallel, perpendicular, or neither.**

**I can write equations of parallel lines and perpendicular lines.**

**parallel lines** - lines in the same plane that never intersect

**perpendicular lines** - lines that intersect to form right angles

**opposite reciprocals** - two numbers whose product is  $-1$

I can determine whether lines are parallel, perpendicular, or neither.  
I can write equations of parallel lines and perpendicular lines.

take note

## Key Concept Slopes of Parallel Lines

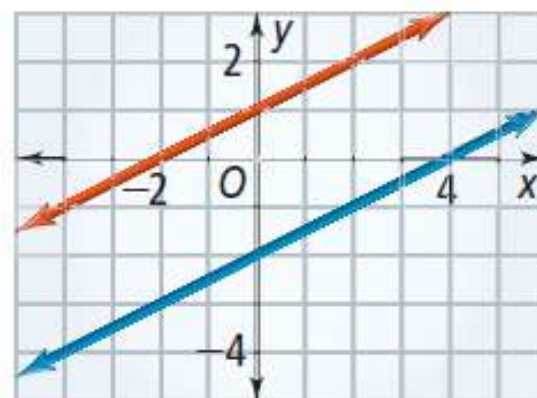
### Words

Nonvertical lines are parallel if they have the same slope and different  $y$ -intercepts. Vertical lines are parallel if they have different  $x$ -intercepts.

### Example

The graphs of  $y = \frac{1}{2}x + 1$  and  $y = \frac{1}{2}x - 2$  are lines that have the same slope,  $\frac{1}{2}$ , and different  $y$ -intercepts. The lines are parallel.

### Graph



I can determine whether lines are parallel, perpendicular, or neither.

I can write equations of parallel lines and perpendicular lines.



### Problem 1

### Writing an Equation of a Parallel Line

A line passes through  $(12, 5)$  and is parallel to the graph of  $y = \frac{2}{3}x - 1$ . What equation represents the line in slope-intercept form?

**I can determine whether lines are parallel, perpendicular, or neither.**

**I can write equations of parallel lines and perpendicular lines.**

1. A line passes through  $(-3, -1)$  and is parallel to the graph of  $y = 2x + 3$ .  
What equation represents the line in slope-intercept form?

I can determine whether lines are parallel, perpendicular, or neither.  
I can write equations of parallel lines and perpendicular lines.

take note

### Key Concept Slopes of Perpendicular Lines

#### Words

Two nonvertical lines are perpendicular if the product of their slopes is  $-1$ . A vertical line and a horizontal line are also perpendicular.

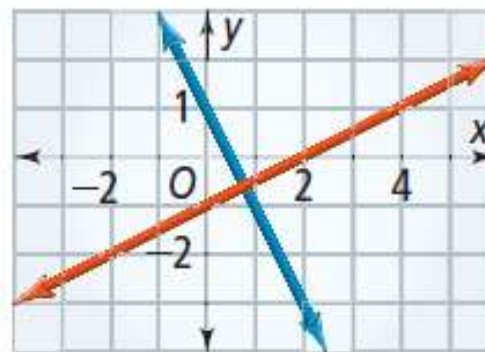
#### Example

The graph of  $y = \frac{1}{2}x - 1$  has a slope of  $\frac{1}{2}$ .

The graph of  $y = -2x + 1$  has a slope of  $-2$ .

Since  $\frac{1}{2}(-2) = -1$ , the lines are perpendicular.

#### Graph



Two numbers whose product is  $-1$  are **opposite reciprocals**. So, the slopes of perpendicular lines are opposite reciprocals. To find the opposite reciprocal of  $-\frac{3}{4}$ , for example, first find the reciprocal,  $-\frac{4}{3}$ . Then write its opposite,  $\frac{4}{3}$ . Since  $-\frac{3}{4} \cdot \frac{4}{3} = -1$ ,  $\frac{4}{3}$  is the opposite reciprocal of  $-\frac{3}{4}$ .

I can determine whether lines are parallel, perpendicular, or neither.  
I can write equations of parallel lines and perpendicular lines.



## Problem 2 Classifying Lines

Are the graphs of  $4y = -5x + 12$  and  $y = \frac{4}{5}x - 8$  *parallel, perpendicular, or neither*? Explain.

I can determine whether lines are parallel, perpendicular, or neither.

I can write equations of parallel lines and perpendicular lines.

2. Are the graphs of the equations *parallel*, *perpendicular*, or *neither*? Explain.

a.  $y = \frac{3}{4}x + 7$  and  $4x - 3y = 9$



I can determine whether lines are parallel, perpendicular, or neither.  
I can write equations of parallel lines and perpendicular lines.



### Problem 3 Writing an Equation of a Perpendicular Line

**Multiple Choice** Which equation represents the line that passes through (2, 4) and is perpendicular to the graph of  $y = \frac{1}{3}x - 1$ ?

(A)  $y = \frac{1}{3}x + 10$

(B)  $y = 3x + 10$

(C)  $y = -3x - 2$

(D)  $y = -3x + 10$

**I can determine whether lines are parallel, perpendicular, or neither.**

**I can write equations of parallel lines and perpendicular lines.**

3. A line passes through  $(1, 8)$  and is perpendicular to the graph of  $y = 2x + 1$ . What equation represents the line in slope-intercept form?

## Lesson Check

### Do you know **HOW**?

1. Which equations below have graphs that are parallel to one another? Which have graphs that are perpendicular to one another?

$$y = -\frac{1}{6}x$$

$$y = 6x$$

$$y = 6x - 2$$

2. What is an equation of the line that passes through  $(3, -1)$  and is parallel to  $y = -4x + 1$ ? Give your answer in slope-intercept form.
3. What is an equation of the line that passes through  $(2, -3)$  and is perpendicular to  $y = x - 5$ ? Give your answer in slope-intercept form.

## Lesson Check

### Do you know HOW?

1. Which equations below have graphs that are parallel to one another? Which have graphs that are perpendicular to one another?

$$y = -\frac{1}{6}x$$

$$y = 6x$$

$$y = 6x - 2$$

2. What is an equation of the line that passes through  $(3, -1)$  and is parallel to  $y = -4x + 1$ ? Give your answer in slope-intercept form.
3. What is an equation of the line that passes through  $(2, -3)$  and is perpendicular to  $y = x - 5$ ? Give your answer in slope-intercept form.

### Lesson Check

1.  $y = 6x$  and  $y = 6x - 2$ ;  $y = -\frac{1}{6}x$   
and  $y = 6x$ ,  $y = -\frac{1}{6}x$  and  
 $y = 6x - 2$
2.  $y = -4x + 11$
3.  $y = -x - 1$